

Subject - Physics / By - Uday SinghConstructive Beats: -

The maximum value of the amplitude  
 $A = \pm 2a$ , then

$$\cos 2\pi \left( \frac{n-m}{2} \right) t = \pm 1$$

∴,  $\pi (n-m) t = k\pi$ , where  $k = 0, 1, 2, 3, \dots$

$$\therefore, t = \frac{k}{n-m} = 0, \frac{1}{n-m}, \frac{2}{n-m}, \frac{3}{n-m}, \dots$$

and so on i.e.  $t$  is an integral multiple of  $\frac{1}{n-m}$

The time value between two consecutive maxima =  $\frac{1}{n-m}$ .

The frequency of maxima =  $n-m$

The maximum value of the amplitude  $A = 0$

When,  $\cos 2\pi \left( \frac{n-m}{2} \right) t = 0$

∴,  $\pi (n-m) t = k\pi + \pi/2$ , where  $k = 0, 1, 2, 3, \dots$

$$\therefore, t = \frac{k}{2(n-m)} + \frac{1}{2(n-m)}$$

$$= \frac{1}{2(n-m)} + \frac{3}{2(n-m)} + \frac{5}{2(n-m)} + \dots$$

∴  $k = 1, 2, 3, \dots$  and so on i.e.,  
 $t$  is the odd multiple of  $\frac{1}{2(n-m)}$

The maxima are, therefore, regularly timed between the maxima. The time interval between consecutive minima

$$= \frac{1}{n-m}$$

∴ The frequency of minima,  
 $= n-m$

Since, one maximum and one minimum sound constitutes a beat, the no. of beats =  $n-m$ . The intensity of the resultant sound rises and falls  
 $= n-m$  times per second.